THE BALLUTE: A RETARDATION DEVICE AND WIND SENSOR

By

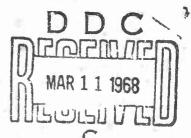
Jamos K. Luers

University of Dayton Research Institute Dayton, Ohio

Contract AF 19(628)-4796
Task No. 6682
Project No. 668204
Work Unit No. 6682C401

Scientific Report No. 3

November 1967



Contract Monitor: Robert W. Lenhard Aerospace Instrumentation Laboratory

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Prepared for

AIR FORCE CAMBRIDGE RESEARCH LABORATORIES
OFFICE OF AEROSPACE RESEARCH
UNITED STATES AIR FORCE
BEDFORD, MASSACHUSETTS 01730



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ABSTRACT

Experimental tests have been made with various configurations of the BALLUTE in order to develop a stable retardation device for meteorological rocketsondes. This report discusses the reduction and analysis of these tests. Several of the BALLUTE configurations are shown to satisfy the project goal of providing the required stability as well as a sufficiently slow fall velocity to accurately measure winds and temperature.

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SECTION I

INTRODUCTION

Two types of BALLUTE configurations are presently being tested and evaluated as retardation devices for Meteorological Rocketsondes. The two configurations are the 8 or 12-gore, 14-16 foot diameter BALLUTEs designed for use with the Arcasonde meteorological package and the light weight 4, 6, or 12-gore, 6-7 foot diameter BALLUTEs designed to be used with the Loki-Dartsonde package.

The mission of both BALLUTE configurations is to provide a stable retardation of the sonde during its descent from rocket apogee (approximately 200, 000 ft) to 80,000 feet. Freedom from large coning angles experienced with the more conventional silk parachutes will result in cleaner telemetry reception. A slower fail rate is also desirable since it will allow the BALLUTE more time to sense the atmosphere and thus temperature and winds can be measured to a higher degree of accuracy. In order to attain the te objectives design requirements demand that the BALLUTE be aerodynamically a very stable object and further that its fall velocity be sufficiently slow. Sufficiently slow is taken to mean a maximum vertical velocity of 300 ft/second at 180,000 feet or a ballistic coefficient value of W/CDA = 0.50. Slower fall rates are, of course, desirable.

SECTION II

LOG OF FLIGHTS

BALLUTE Arcasonde and Dartsonde flights began in April of 1966 at Cape Kennedy. A log of the succe of lights and their characteristics are given in Table 1.

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	lbs.	Total Weight		1.06	1.07	1.07	1.10	7.06		7.71	7.90		7. 37		6.48	6.47	8.17	8. 17		1.00	1,056	1.0	6.78		6.7		7.9	1.18	7.89	1. 98	1.12	1. 12	7.96	7.99	7.9	7.97	1.09	7.64	7.64	1.09	1.09	1.09
	.∎q[Sonde Weight		74	. 75	. 75	. 78	4.63		4.63	4.63		4.63		3,3	3,3	4.63	4.63		. 74	- 74	7.	3,3		3,3		4.63	- 74	4.63	.74	. 74	. 74	4.63	4.63	4.63	4.63	. 74	4.63	4.63	. 74	. 74	. 74
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CHARACTERISTICS		9840	1/4	1/4	1/4	1/4	1/4	1/4		1/2	1/2		1/2		1/2	1/2	1/2	1/2		1/4	1,4	1/4	1/2		1/2		7/1	1/4	1/2	1/4	1/4	1/4	1/2	1/2	1/2	1/2	1/4	1/2	1/2	1/4	1/4	1/4
BALLUTE	.33	Size Otem.		9	9	9	9	16		12 1/2	7		<u>+</u>		1.	14	15	7:		6 1/2	Ş	6 1/2	15		15			6 1/2	15	6 1/2	~	_	S	Ś	7	15 1/2	7		15 1/2	2	7	7
BA		Ballute Series	Dart 2			Dart 5	Dart 7	Arcas 6		Arcas 9	Arcas 10		Arcas 11		Arcas 12	Arcas 13	Arcas 14	Arcas 15		Dart 11	Dart 12	Dart 13	Arcas	extra	Arcas		Arcas 16	Dart 15	Arcas 17	Dart 16	Dart 17	Dart 18	Arcas 18	Arcas 19	Arcas 20	Arcas 21	Dart 21	Arcar 22	Arcas 23	Dart 23	2	Dart 25
		Flight Date	04-22-66	-24-6	05-26-66	05-27-66	99-90-20	07-08-66	07-08-66	08-15-66	08-16-66	08-16-66	08-18-66	09-14-66	09-14-66	99-11-60	39-61-60	99-50-60		11-14-66	11-14-66	11-15-66	11-17-66		11-18-66		01-30-66	٠ -3	01-31-67	01-31-67	02-27-67	19-87-20	03-01-67	03-02-67	04-12-67	04-19-67	29-60-50	05-10-67	65-10-67	05-12-67	-12	05-18-67
		Time	1606	1500	1838	1445	1615	1509	1630	1500	1500	1600	1500	1359	1830	1600	1500	1500		1900	2002	1520	1920		1830		1430	1703	1500	1608	1500	1630	1500	1600	1500	1500	1421	1500	1600	1527	1627	1115
	j	Type o	Ballute	Ballute	Ballute	Ballute	Ballute	Ballute	Parachute	Ballute	Ballute	Parachute	Ballute	Parachute	Ballute	Ballute	Ballute	Ballute	Parachute	Ballute	Ballute	Ballute	Ballute		Ballute		Ballute	Ballute	Ballute	Ballute	Ballute	Ballute	Ballute	Ballute	Ballute	Ballute	Ballute	Ballute	Ballute	Ballute	Ballute	Ballute
	ı	Flight Numbe	3084	2643	2561	2793	9060	0715	7683	7391	5554	2609	1867	2419	1692	3163	1947	1731	3309	4765	3166	6258	4287		3720		1152	0015	2694	6600	1616	0613	0776	7092	3605	0739	5395	8990	8622	8767	6513	8534

SECTION III

DATA REDUCTION

The data from the successful flights were reduced at UDRI. The reduced data were presented in the form of a blue data booklet for each flight. The format of the booklet and what it contains follow.

Title Page -- Contains launch and flight log information as well as any special comments concerning performance of the sonde and radars.

Tabulations -- As many as five (5) sets of tabulations may be contained in a booklet if all temperature information is available. The first tabulation gives the component velocity and acceleration of the BALLUTE as obtained by a 39-7 linear linear least squares fit. The second tabulation computes the ballistic coefficient using the temperature from the strip chart, and the vertical velocity obtained from the first tabulation. The remaining tabulations contain the rawin onde flight of the day and the Cape Kennedy BALLUTE reduction of winds and density.

Plots -- If temperature data is available, three types of plots are presented in the booklets; a) vertical velocity vs altitude, b) temperature vs altitude, and c) density vs altitude. If the temperature trace is poor or not available only the vertical velocity vs altitude plot is included.

Table 2 shows the content of each data booklet that was reduced by UDRI.

Cape Kennedy Reduction

			1	TABLE 2			pul			
			BALLUTE	DATA BOOK	KLETS		ure a Plot		ure	e q
Flight Number	Type of Flight	Time Zulu	Flight Date	Ballute Series	Accel Data	ocity eration From	Temperature and Density Plots	Winds	Temperature	Rawinsonde
3084	Ballute	1606	04-22-66	Dart 2		19.18	x	х		
2643	Ballute	1500	05-24-66	Dart 3	1.16	-,,	X	X		
2561	Ballute	1838	05-26-66	Dart 4	1.16		X	X		X
2793	Ballute	1445	05-27-66	Dart 5	1.16		x			
0906	Ballute	1615	07-06-66	Dart 7	1. 16	1.4	x			x
0715	Ballute	1509	07-08-66	Arcas 6	1. 16	1.3	X	X	X	x
7683	Parachute	1630	07-08-66	111000	1.16	1.4		X		
7391	Ballute	1500	08-15-66	Arcas 9	1. 16		X	x	X	x
5554	Ballute	1500	08-16-66	Arcas 10	1.16		X		X	x
6097	Parachute	1600	08-16-66		1.16		X	X	X	x
7867	Ballute	1500	08-18-66	Arcas 11		19.16	X		X	x
2419	Parachute	1359	09-14-66		1.16					x
2691	Ballute	1830	09-14-66	Arcas 12	1.16		X		X	x
1615	Parachute	1359	09-15-66		1.16	1.3				X
3163	Ballute	1600	09-15-66	Arcas 13	1.16	1.4	X			X
1947	Ballute	1500	09-19-66	Arcas 14	1.16	1.3	X		X	X
1731	Ballute	1500	09-20-66	Arcas 15	1.16		X		X	
3309	Parachute				1.16					
4765	Ballute	1900	11-14-66	Dart 11	1.16	1.5				X
3166	Ballute	2007	11-14-66	Dart 12	1.16	1.5				x
6258	Ballute	1520	11-15-66	Dart 13	1.16					
4287	Ballute	1920	11-17-66	Arcas	1.16	1.4	X		X	X
3729	Ballute	1830	11-18-66	Arcas	1.16	1.4				
2577	Ballute	1430	01-30-67	Arcas 16	1.16	1.4				
0015	Ballute	1703	01-30-67	Dart 15	1.16	1.4				
2694	Ballute	1500	01-31-67	Arcas 17	1.16	Mod II				
0099	Ballute	1608	01-31-67	Dart 16	1.16	Mod II				
1616	Ballute	1500	02-27-67	Dart 17	1.16	Mod II				
0613	Ballute	1630	02-28-67	Dart 18	1.16					
0776	Ballute	1500	03-01-67	Arcas 18	1.16	Mod II				
7092	Ballute	1600	03-02-67	Arcas 19	1.16	1.5				
3605	Ballute	1500	04-12-67	Arcas 20	1.16	Mod II	X	X	X	X
0739	Ballute	1500	04-19-67	Arcas 21	1.16	1.5	X	X	X	x
5395	Ballute	1421	05-09-67	Dart 21		1.5	X	X	X	X
8990	Ballute	1500	05-10-67	Arcas 22		1.5	X	X	X	X
8622	Ballute	1600	05-10-67	Arcas 23		1.5		X		X
8767	Ballute	1527	05-12-67	Dart 23	1.16	1.5	X	X	X	X
6513	Ballute	1627	05-12-67	Dart 24	1.16	1.5	X	X	X	X
8534	Ballute	1115	05-18-67	Dart 25	1.16	1,5	X	X	X	

SECTION IV

METHOD OF REDUCTION

4.1 Velocity and Acceleration of Ballute

The velocity of the BALLUTE was obtained by a linear least squares fit of 39-1/2 second position points. The slope of the fitted line is called the velocity at the midpoint in time of the interval. If the radar records at increments less than 1/2 second then these position points are averaged to obtain 1/2 second increments between consecutive coordinates. To obtain an acceleration, seven (7) velocities are fitted linearly and the slope assigned to the midpoint as the acceleration. To obtain derivatives each second one slides two position coordinates and one velocity coordinate and repeats the fitting procedure. For a further description see Engler 1965.

4.2 Temperature

Temperature was either read directly from the strip chart or if it had already been reduced it was interpolated from the reduced data at altitude increments of 1000 feet.

4.3 Density

The density was calculated from temperature by using the Gas Law and Hydrostatic Equation. The formula is

$$\ell_{n}(\rho_{n}) = \ell_{n}(\rho_{0}) - \ell_{n}(\frac{T}{T_{0}}) - \frac{1}{K} \int_{Z_{0}}^{Z_{n}} \frac{|g|}{T} dz \text{ (See Appendix)} \quad (1)$$

where ρ_0 = initial density - obtained from rawinsonde flight for the day

T = Temperature

K = Gas constant/molecular weight of atmosphere

g = gravitational acceleration

The integration started with the lowest BALLUTE altitude and proceded upwards so that the initial density (ρ_0) could be taken from the rawinsonde flight for that day.

4.4 Ballistic Coefficient

The ballistic coefficient is computed from the equation

$$q = \frac{\rho \dot{Z}^2}{2}$$

where q = ballistic coefficient

Z = vertical velocity.

SECTION V

ANALYSIS

5.1 Wind

Computation of horizontal winds has not been included in the present reduction of BALLUTE flights. The following analysis is designed to determine the necessity and importance of the acceleration and apparent mass of the BALLUTE in a wind computation.

Ignoring the Coriolis force and the buoyancy of the payload, the equations of motion in the X and Z direction for the BALLUTE can be written as:

$$(m_p + m_g) \ddot{X} = \frac{1}{2} \rho C_D AV (W_x - \dot{X}) + m' (\dot{W}_x - \ddot{X})$$
 (2)

$$(m_p + m_g) \ddot{Z} = \frac{1}{2} \rho C_D AV (W_z - \dot{Z}) + m' (\dot{W}_z - \dot{Z}) - m_p |g|$$
 (3)

where

m_p = mass of BALLUTE plus payload

mg = mass of gas

m' = apparent mass of BALLUTE

C_D = Drag Coefficient

A = Cross sectional area of BALLUTE

$$v = [(\dot{x} - w_x)^2 + (\dot{z} - w_z)^2]^{1/2}$$

Assuming the absence of vertical winds, Equation (2) and (3) are combined to give the wind equation:

$$W_{x} - K_{2} \dot{W}_{x} = \dot{X} - K_{1} \dot{X}$$
 (4)

where

$$K_{1} = \frac{(m_{p} + m_{g} + m') \dot{Z}}{(m_{p} + m_{g} + m') \dot{Z} + m_{p} |g|} \quad K_{2} = \frac{m' \dot{Z}}{(m_{p} + m_{g} + m') \dot{Z} + m_{p} |g|}$$

If the wind equation is written as $\mathbf{W}_{\mathbf{x}} = \dot{\mathbf{X}} - \mathbf{K}_{1} \ddot{\mathbf{X}} + \mathbf{K}_{2} \ddot{\mathbf{W}}_{\mathbf{x}}$ then the component terms on the right hand side of this equation can be plotted for a given wind field to determine their contribution to $\mathbf{W}_{\mathbf{x}}$. The term: $\dot{\mathbf{X}}$ represents the velocity of the BALLUTE; $\mathbf{K}_{1} \ddot{\mathbf{X}}$ represents the contribution to $\mathbf{W}_{\mathbf{x}}$ as seen by the acceleration of the BALLUTE; and $\mathbf{K}_{2} \ddot{\mathbf{W}}_{\mathbf{x}}$ represents the contribution to $\mathbf{W}_{\mathbf{x}}$ due to the apparent mass of the BALLUTE.

Consider a Sinusoidal Wind Field

Figures 1-4 are plots of the component terms of the wind equation for the wind field $W_x = A \sin{(\frac{2\pi Z}{2000})}$. From the plots it is seen that the term K_2 \dot{W}_x contributes less than 1/2% to the amplitude. K_2 , however, was computed using $m' = 1/2 \rho$ Vol which is the apparent mass formula for a sphere. This assumption was necessary due to the lack of knowledge concerning the apparent mass of the BALLUTE. Even if the formula were considerably in error the apparent mass term would still not be a significant term in the wind equation. The acceleration term $K_1\dot{X}$, however, is significant, particularly at high altitudes. It is also seen from the plots that the Dartsonde BALLUTE is slightly more wind sensitive than the Arcasonde BALLUTE. This is due to its slower fall velocity and smaller ballistic coefficient (see Table 3).

Consider a Linear Wind Field

The sensing ability of the BALLUTE can also be analyzed under the influence of a linear wind field. Figures 5 and 6 compare Arcasonde BALLUTE velocity to wind velocity for linear winds with shear values from .013 to .1 per sec. In all cases, BALLUTE velocity is not an accurate measure of wind velocity and consequently the acceleration of the BALLUTE must be included in any wind computation. It can easily be shown that the apparent mass term is insignificant for a linear wind field as well as for a sinusoidal field.

Hence accurate winds can be determined only if velocity and accelerations are measured accurately. Initially, velocity and acceleration have been obtained from the 39-7 linear fit. This technique was used as a result of our previous experience with the ROBIN system taking into consideration the slower vertical velocity of the BALLUTE by lengthening the position smoothing interval from 31 to 39 points. It is not believed that this will ultimately be the smoothing technique decided upon to compute velocities and accelerations and thus calculate a wind. Indications are that the vertical smoothing interval should not necessarily be of the same length as the horizontal. Also in some cases a cubic velocity fit may improve upon a linear fit.

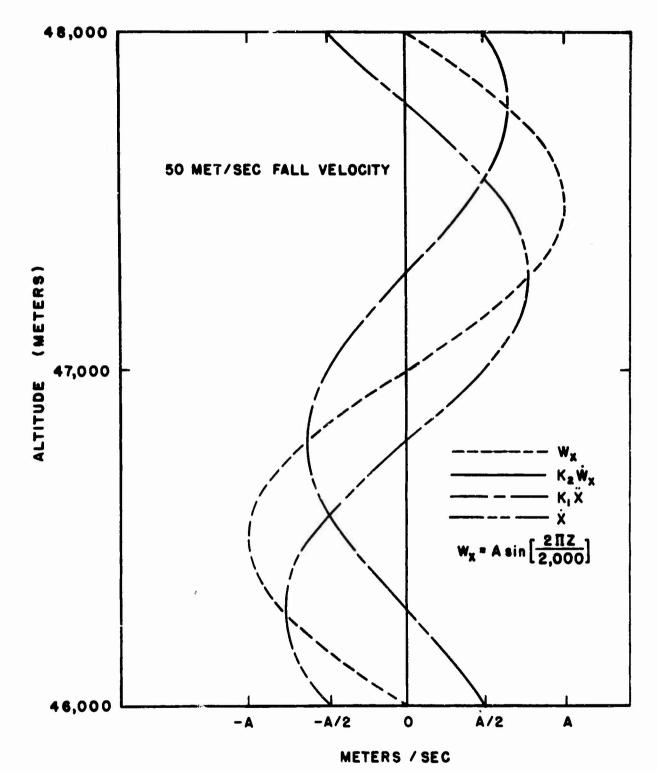


Figure 1. Response of Arcasonde BALLUTE to Sinusoidal Wind Field
10

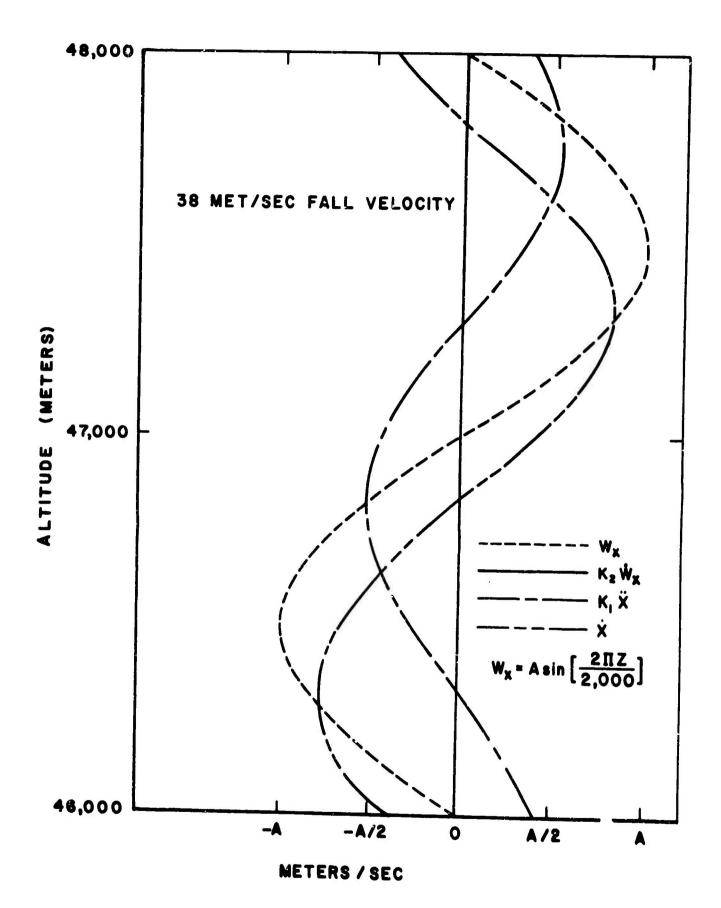


Figure 2. Response of Dartsonde BALLUTE to Sinusoidal Wind Field

11

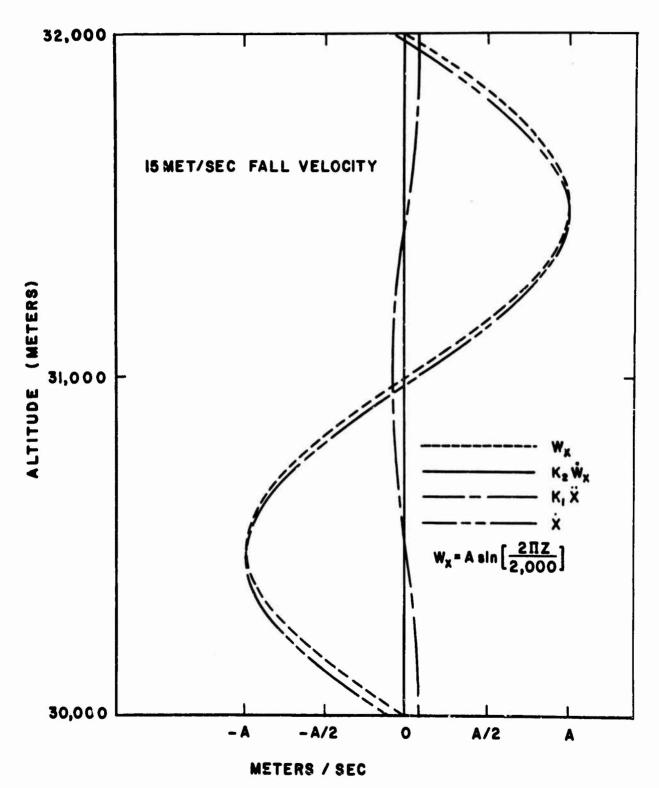


Figure 3. Response of Arcasonde BALLUTE to Sinusoidal Wind Field

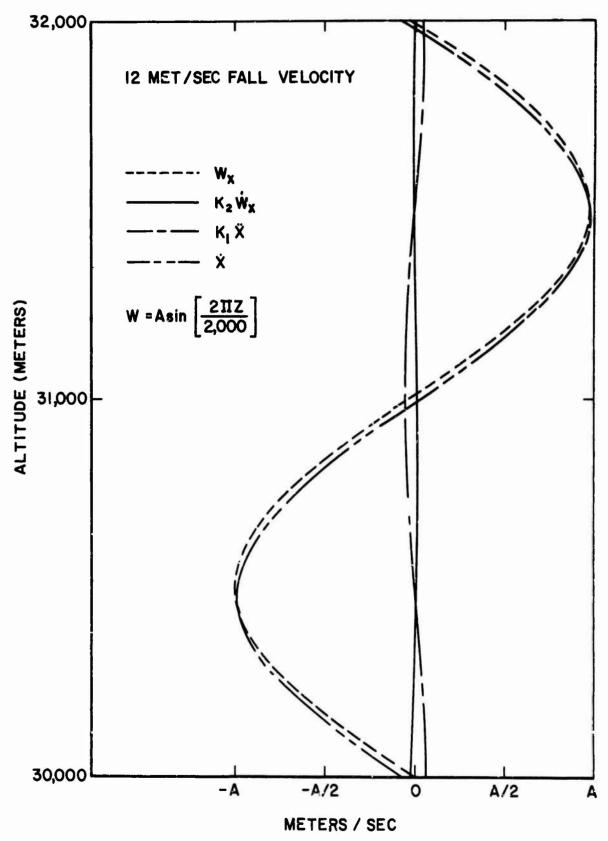
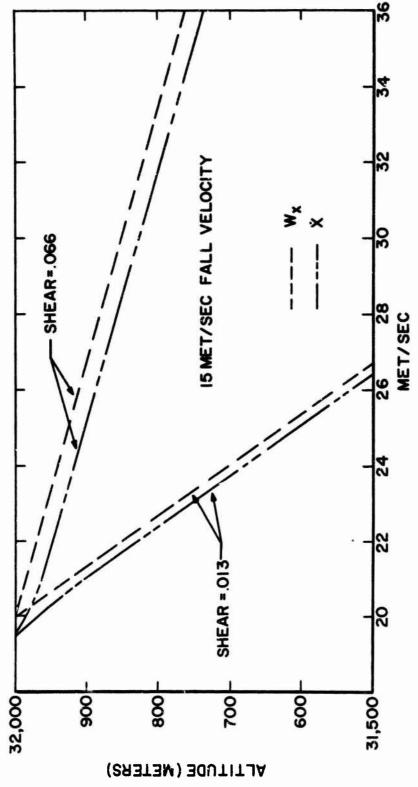


Figure 4. Response of Dartsonde BALLUTE to Sinusoidal Wind Field



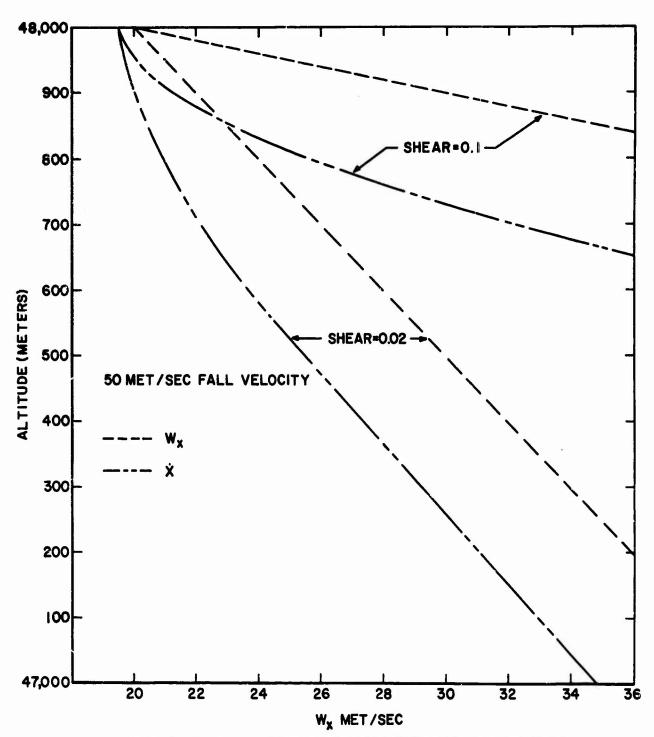


Figure 6. Response of Arcasonde BALLUTE to Linear Wind Field

5. 2 Ballistic Coefficient

In order to insure an acceptable fall rate the BALLUTE has a design criterion of maintaining a maximum ballistic coefficient of $q = \frac{W}{C_D A} = 0.050$. The ballistic coefficient equation is derived from the vertical equation of motion as follows:

$$(m_p + m_g)\ddot{Z} = \frac{1}{2} \rho C_D AV (W_z - \dot{Z}) + m' (\dot{W}_z - \ddot{Z}) - m_p |g|$$

If over a sufficiently small interval Z can be considered constant and $W_{z} = 0$ the equation simplifies to:

$$\frac{\mathbf{m}_{\mathbf{p}} |\mathbf{g}|}{\mathbf{C}_{\mathbf{p}} \mathbf{A}} = -\frac{1}{2} \rho \mathbf{V} \dot{\mathbf{Z}}. \tag{5}$$

The common formula for ballistic coefficient

$$q = \frac{m_p |g|}{C_D A} = \frac{1}{2} \rho \dot{Z}^2$$
 (6)

is obtained by further assuming that $V = \dot{Z}$. This assumption is valid except for the first 3000 feet of descent. During this period the BALLUTE has a large horizontal velocity transmitted to it from the rocket, and thus its velocity relative to the air may be much larger than \dot{Z} .

In the data booklets two methods have been used to evaluate q.

Method 1

From the thermistor temperature trace the density is computed by Equation (1), \dot{Z} is obtained from the 39-7 linear fit, and q is then computed as $q = \frac{1}{2} \rho \dot{Z}$. A ballistic coefficient is computed by this method at each 1000 feet of altitude.

Method 2

The second method of calculating a ballistic coefficient assumes that the BALLUTE fell in the 1962 Standard Atmosphere. For a given ballistic coefficient (q) a \dot{Z} vs Z curve is generated from Equation (3) by obtaining density as a function of altitude from the 1962 Standard Atmosphere. A series of these \dot{Z} vs Z curves are generated for values of q from q = 0.01 to q = 0.10.

From a reduced BALLUTE flight a plot is made of \dot{Z} vs Z. This velocity profile of the BALLUTE is then compared to the ballistic coefficient curves. The curve that most closely follows the BALLUTE velocity profile is considered a representative value for q. It has been experimentally varified by both Method 1 and Method 2 that the value of q is relatively constant over the entire flight. If the atmosphere is not model an error will be made using Method 2 to compute a ballistic coefficient. For example if density is only 80% of Model, then

$$q_{\text{True}} = \frac{1}{2} (0.8 \, \rho_{\text{Model}}) \dot{Z}^{2}$$

$$q_{\text{Method 2}} = \frac{1}{2} (\rho_{\text{Model}}) \dot{Z}^{2}$$

$$m_{\text{Error}} = \frac{\left| q_{\text{True}} - q_{\text{Method 2}} \right|}{q_{\text{True}}} = \frac{\frac{1}{2} (0.2 \, \rho_{\text{Model}}) \dot{Z}^{2}}{\frac{1}{2} (0.8 \, \rho_{\text{Model}}) \dot{Z}^{2}} = 25\%.$$

Table 3 gives the ballistic coefficient for each flight as determined by both methods. The 12-gore Dartsonde BALLUTEs show a somewhat smaller ballistic coefficient (.045) than the 12-gore Arcasonde BALLUTEs (.05). However, a later series of firing using a 4-gore Dartsonde BALLUTE and 8-gore Arcasonde BALLUTEs have produced a substantial decrease in the ballistic coefficient. An average value of ballistic coefficient for the 4-gore Dartsonde BALLUTE is 0.035 and the 8-gore Arcasonde BALLUTE 0.04. These ballistic coefficients provide the required descent rate.

5.3 Temperature

In order to insure an accurate measure of temperature, a) the vertical velocity of the BALLUTE must be sufficiently slow to insure that induced aerodynamic heating is negligible and b) the BALLUTE is aerodynamically a stable vehicle so that the system does not oscillate or come through wide angles thus resulting in aerodynamic heating of the thermistor as well as signal dropouts. The established vertical velocity criterion is to maintain a ballistic coefficient ≤ 0.05. As can be seen by Table 3, BALLUTEs achieve this result in nearly all cases. The stability condition has been verified by an observation of position plots as well as the temperature strip chart which shows very few signal dropouts. (See Wright and Graham, 1966.) Figures 7-12 are North-East position plots of flight 906. Throughout the entire flight path there is no evidence of any periodic aerodynamic oscillation in the BALLUTE's path. The very smooth path prevalent over several large segments also substantiates the stability of the BALLUTE.

TABLE 3
BALLISTIC COEFFICIENTS

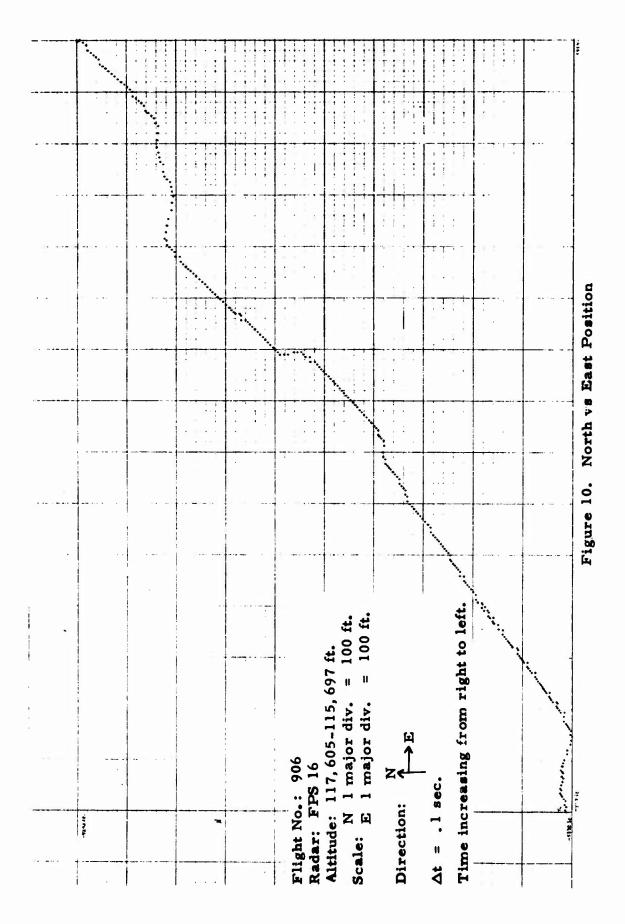
Flight	Туре	Time	Flight	Ballute	Ballistic	Coefficient
Number	of Flight	Zulu	Date	Series	Method 1	Method 2
3084	Ballute	1606	04-22-66	Dart 2		. 05
2643	Ballute	1500	05-25-66	Dart 3	. 035 045	. 045
2561	Ballute	1838	05-26-66	Dart 4	.0405	. 045
2793	Ballute	1445	05-27-66	Dart 5	.0607	~ 065
0906	Ballute	1615	07-06-66	Dart 7	. 035 04	. 04
1715	Ballute	1509	07-08-66	Arcas 6	.0407	. 04 06
7683	Parachute	1630	07-08-66			. 05 07
7391	Ballute	1500	08-15-66	Arcas 9	.0809	.08
5554	Ballute	150C	08-16-66	Arcas 10	. 055 065	. 06
6097	Parachute	1600	08-16-66		.0405	. 05.5
7867	Ballute	1500	08-18-66	Arcas 11	. 05 06	.055
2419	Parachute	1359	09-14-66			. 04
2691	Ballute	1830	09-14-66	Arcas 12	. 05 06	. 05
1615	Parachute	1359	09-15-66			. 05
3163	Ballute	1600	09-15-66	Arcas 13	. 05	. 05
1947	Ballute	1500	09-19-66	Arcas 14	. 045 05	. 05
1731	Ballute	1500	09-20-66	Arcas 15	. 05	. 05
3309	Parachute					. 05
4765	Ballute	1900	11-14-66	Dart 11		.04
3166	Ballute	2007	11-14-66	Dart 12		. 045
6258	Ballute	1520	11-15-66	Dart 13		.035
4287	Ballute	1920	11-17-66	Arcas	. 05 06	. 05
				extra		
3729	Ballute	1830	11-18-66	Arcas		. 05
				extra		
2577	Ballute	1430	01-30-67	Arcas 16		. 06
0015	Ballute	1703	01-30-67	Dart 15		. 05
2694	Ballute	1500	01-31-67	Arcas 17		. 055
ა099	Ballute	1608	01-31-67	Dart 16		. 035
1616	Ballute	1500	02-27-67	Dart 17		.035
0613	Ballute	1630	02-28-67	Dart 18		.035
0776	Ballute	1500	03-01-67	Arcas 18		.015
7092	Ballute	1600	03-02-67	Arcas 19		. 01 1
3605	Ballute	1500	04-12-67	Arcas 20	.0405	. 04 055
0739	Ballute	1500	04-19-67	Arcas 21	.0405	. 05
5395	Ballute	1421	05-09-67	Dart 21		
8990	Ballute	15 0 0	05-10-67	Arcas 22	.04	.045
8622	Ballute	1600	05-10-67	Arcas 23		
8767	Ballute	1527	05-12-67	Dart 23	. 025 03	.025
6513	Ballute	1627	05-12-67	Dart 24	. 025 03	. 03
8534	Ballute	1115	05-18-67	Dart 25	. 035	. 035

Figure 7. North vs East Position

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700									
Flight No.: 906 Radar: FPS 16 Altitude: 134, 115-132, 848 ft. N 1 major div. = 100	.132, 848 ft. div. = 100 ft				-				
Scale: E 1 major div. Direction: N	div. = 100 ft.								-
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Time increasing from right to	com right to left.	•							•

Figure 8. North vs East Position

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Figure 11. North vs East Position

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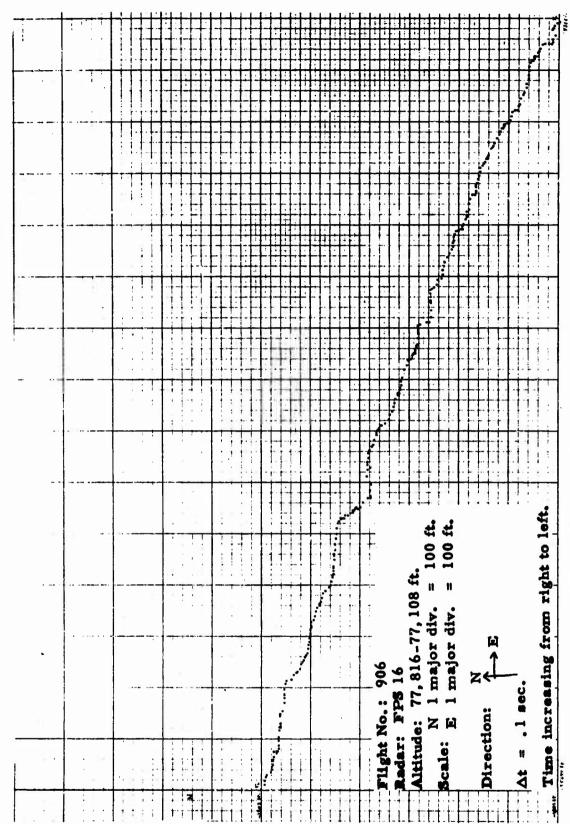


Figure 12. North vs East Position

5.4 Density

Density is obtained from temperature by use of Equation (1). The integral is evaluated by use of the trapezoidal rule (see Appendix). Integration by the trapezoidal rule assumes a linear interpolation of temperature between data points, which for the purposes of reduction were read every 1000 feet.

The initial density required for Equation (1) is obtained from the rawinsonde flight for the day of launch. If the initial density is in error by e₀ this will introduce a constant percentage error in density for the entire flight given by:

% Error =
$$\frac{e_0}{\rho_0}$$
. (See Appendix.)

SECTION VI

CONTINUING INVESTIGATION OF BALLUTE AS WIND SENSOR

Future investigation at UDRI will be directed towards determining an optimum method to compute winds and the resulting error in winds as a function of radar error using this method. The UDRI is presently developing and evaluating smoothing methods for obtaining velocity and acceleration using the criterion of a minimization of the total error in the wind. The total error is defined as: $\sigma_T^2 = \sigma_{Fit}^2 + \sigma_{Noise}^2 \text{ where } \sigma_{Noise}^2$ is the random error in wind due to the noise in the position coordinates and $\sigma_{Fit}^2 = \sigma_{Fit}^2 + \sigma_{Noise}^2 = \sigma_{Noise}^2$ function. The UDRI also is investigating the effect of the radar range resolver error on wind determination. Considerable work has already been done with regards to these two aspects on the High Altitude ROBIN, and ROSE systems. Much of this work can be applied to the BALLUTE system.

APPENDIX

DENSITY OBTAINED FROM A TEMPERATURE PROFILE

I.

- 1) p = KρT Gas Law
- 2) $dp = -\rho |g| dZ$ Hydrostatic Equation

where

p = pressure

 $\rho = density$

T = Temperature

g = gravitational acceleration

Z = Altitude

K = Universal Gas Constant/Molecular weight of atmosphere

From Equation (1)

$$dp = K \rho dT + KT dp$$

substituting into Equation 2 we get

$$-\rho |g| dZ = K \rho dT + KT d\rho$$
.

Simplifying

$$\frac{d\rho}{\rho} = -\frac{|g|}{KT} dZ - \frac{dT}{T}$$

Initial Conditions:

At Z =
$$Z_0$$
, g = g_0 , T = T_0 , ρ = ρ_0

At
$$Z = Z_n$$
, $g = g_n$, $T = T_n$, $\rho = \rho_n$

Integrating down from the initial altitude Z_0 we get;

$$\int_{\rho_0}^{\rho_n} \frac{d\rho}{\rho} = -\int_{T_0}^{T_n} \frac{dT}{T} - \frac{1}{K} \int_{Z_0}^{Z_n} \frac{lgl}{T} dZ$$

or

$$\operatorname{Ln}(\rho_n) = \operatorname{Ln}(\rho_0) - \operatorname{Ln}(\frac{T}{T_0}) - \frac{1}{K} \int_{Z_0}^{Z_n} \frac{|g|}{T} dZ$$

Assuming a linear interpolation of temperature between data points, the integral is evaluated by the trapezoidal rule.

$$L_{n}(\rho_{n}) = L_{n}(\rho_{0}) - L_{n}(\frac{T_{n}}{T_{0}}) - \frac{1}{2K} \left[\left(\frac{g_{0}}{T_{0}} + \frac{g_{1}}{T_{1}} \right) (Z_{1} - Z_{0}) + \dots + \left(\frac{g_{n-1}}{T_{n-1}} + \frac{g_{n}}{T_{n}} \right) (Z_{n} - Z_{n-1}) \right]$$

II. Error Due to the Initial Guess of ρ_0

Let e_0 be the error in the initial guess of ρ_0 . Then the computed value of ρ_n is obtained from;

$$L_{n}(\rho_{n}) = L_{n}(\rho_{0} + e_{0}) - L_{n}(\frac{T_{n}}{T_{0}}) - \frac{1}{K} \int_{Z_{0}}^{Z_{n}} \frac{|g|}{T} dZ$$

$$\rho_{n} = (\rho_{0} + e_{0})(\frac{T_{0}}{T_{n}}) \operatorname{Exp}(-\frac{1}{K}) \int_{Z_{0}}^{Z_{n}} \frac{|g|}{T} dZ$$

The percentage error is given by:

$$\% \text{ Error } = \frac{\left| \frac{\rho_{n} \text{ True}^{-\rho_{n} \text{ Compl}}}{\rho_{n} \text{ True}} \right|}{\rho_{n} \text{ True}} = \frac{e_{0} \left(\frac{T_{0}}{T_{n}} \right) \text{ Exp } \left(-\frac{1}{K} \int_{Z_{0}}^{Z_{n}} \frac{|g|}{K} dZ \right)}{\rho_{0} \left(\frac{T_{0}}{T_{n}} \right) \text{ Exp } \left(-\frac{1}{K} \int_{Z_{0}}^{Z_{n}} \frac{|g|}{T} dZ \right)}$$

% Error =
$$\frac{e_0}{\rho_0}$$
 a constant for the entire flight.

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13 ARCTRACT		

Experimental tests have been made with various configurations of the BALLUTE in order to develop a stable retardation device for meteorological rocketsondes. This report discusses the reduction and analysis of these tests. Several of the BALLUTE configurations are shown to satisfy the project goal of providing the required stability as well as a sufficiently slow fall velocity to accurately measure winds and temperature.

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Security Classification

14.	KEY WORDS	LIN	KA	LIN	K B	LIN	КС
	KET WORDS	ROLE	WT	ROLE	WT	ROLE	WT
	BALLUTE)
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	Temperature Sensor						
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